



**IWATE COLLIDER SCHOOL**  
**2024**

**26 FEBRUARY - 2 MARCH, 2024**

Appi highland, Iwate, Japan

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# What is MADGRAPH5\_AMC@NLO?

- It is an **automatic** meta-code that write the code for computing the cross-section and generating events for any process at colliders
- For details

MadGraph 5 : Going Beyond

[1106.0522](#)

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Johan Alwall<sup>(1)</sup>, Michel Herquet<sup>(2)</sup>, Fabio Maltoni<sup>(3)</sup>, Olivier Mattelaer<sup>(3)</sup>, Tim Stelzer<sup>(4)</sup>

The automation of next-to-leading order electroweak calculations

[1804.10017](#)

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R. Frederix,<sup>a</sup> S. Frixione,<sup>b</sup> V. Hirschi,<sup>c</sup> D. Pagani,<sup>a</sup> H.-S. Shao,<sup>d</sup> M. Zaro<sup>e</sup>

- NLO QCD and EW corrections can be included
- Matrix elements of different multiplicities can be combined
  - at LO (CKKW or MLM)
  - at NLO (FxFx or UNLOPS)

The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations

[1405.0301](#)

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J. Alwall<sup>a</sup>, R. Frederix<sup>b</sup>, S. Frixione<sup>b</sup>, V. Hirschi<sup>c</sup>, F. Maltoni<sup>d</sup>, O. Mattelaer<sup>d</sup>, H.-S. Shao<sup>e</sup>, T. Stelzer<sup>f</sup>, P. Torrielli<sup>g</sup>, M. Zaro<sup>hi</sup>

Older (but still useful!) papers:

Alwall, Demin, De Visscher, Frederix, Herquet, [0706.2334](#)

Maltoni, Stelzer, [hep-ph/0208156](#)



# Software prerequisites:

- Python 3.7+ (still compatible with Python 2.7)
- Fortran compiler supporting quadruple precision (for NLO)
  - gfortran v4.6+ OK
- Optional:
  - gnuplot
  - FastJet (FJcore is included in the tarball)
  - LHAPDF
  - Herwig++ / Pythia8
  - ...



# Where do I get it?

- On LaunchPad: <https://launchpad.net/mg5amcnlo>

**5** MadGraph5\_aMC@NLO

Overview Code Bugs Blueprints Translations Answers

Registered 2009-09-15 by [Michel Herquet](#)

MadGraph5\_aMC@NLO is a framework that aims at providing all the elements necessary for SM and BSM phenomenology, such as the computations of cross sections, the generation of hard events and their matching with event generators, and the use of a variety of tools relevant to event manipulation and analysis. Processes can be simulated to LO accuracy for any user-defined Lagrangian, and the NLO accuracy in the case of models that support this kind of calculations -- prominent among these are QCD and EW corrections to SM processes. Matrix elements at the tree- and one-loop-level can also be obtained.

MadGraph5\_aMC@NLO is the new version of both MadGraph5 and aMC@NLO that unifies the LO and NLO lines of development of automated tools within the MadGraph family. It therefore supersedes all the MadGraph5 1.5.x versions and all the beta versions of aMC@NLO.

The standard reference for the use of the code is: J. Alwall et al, "The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations", arXiv:1405.0301 [hep-ph]. In addition to that, computations in mixed-coupling expansions and/or of NLO corrections in theories other than QCD (eg NLO EW) require the citation of: R. Frederix et al, "The automation of next-to-leading order electroweak calculations", arXiv:1804.10017 [hep-ph]. A more complete list of references can be found here: [http://amcatnlo.web.cern.ch/amcatnlo/list\\_refs.htm](http://amcatnlo.web.cern.ch/amcatnlo/list_refs.htm)

Download:

The latest stable release can be downloaded as a tar.gz package (see the right of this page), or through the Bazaar versioning system, using bazaar branch [lp:mg5amcnlo](#)

Installation:

MadGraph5\_aMC@NLO needs Python version 2.6 or 2.7 ; gfortran/gcc 4.6 or higher is required for NLO calculations/simulations.

Getting started:

Run bin/mg5\_aMC and type "help" to learn how to run MadGraph5\_aMC@NLO using the command interface, or run the interactive quick-start tutorial by typing "tutorial". Some third-party packages can be installed using the MG5\_aMC shell command "install". LO generation can also be done directly online at: <http://madgraph.phys.ucl.ac.be> or <http://madgraph.hep.uiuc.edu>

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Configuration Progress

[Configuration options](#)

Downloads

Latest version is 3.1.x

[MG5\\_aMC\\_v3.1.0.tar.gz](#) 

released on 2021-03-25

[All downloads](#)

Announcements

**Release of 3.1.0 on 2021-03-29**

Version 3.x is now out of beta and is the official version of MG5aMC.



# Where do I get it?

- On LaunchPad: <https://launchpad.net/mg5amcnlo>
- `tar -xzf MG5_aMC_v3.5.2.tar.gz`
- `cd MG5_aMC_v3_5_2`
- `./bin/mg5_aMC`



# Some exercises:

- Exercise 1: Top pair production at LO
- Exercise 2: Decay chains
- Exercise 3: Unitarity in gauge theories
- Exercise 4: Initial-state radiation in lepton collisions
- Exercise 5: Higgs production at the ILC



# Exercise I:

## Top pair production at LO

- **Basic questions:**
  - Generate the process (following the tutorial)
  - Which partonic subprocesses contribute?
  - How many Feynman diagrams has each subprocess?
  - Output the code
  - Compute the x-section at the LHC (13.6 TeV) for  $m_t=170$  GeV
- **Extra questions:**
  - Are b-quarks included in the initial state? If not, how can I include them?
  - Are diagrams with photons/Z included? If not, how can I include them? How much does the cross-section change? What is 'WEIGHTED'?
  - Recompute the  $t\bar{t}$  cross-section for  $m_t=170, 172, 174 \dots 180$  GeV



# Exercise 1: solution

- Generate the process (following the tutorial)

- `> generate p p > t t~`

```
INFO: Checking for minimal orders which gives processes.  
INFO: Please specify coupling orders to bypass this step.  
INFO: Trying coupling order WEIGHTED=2  
INFO: Trying process: g g > t t~ WEIGHTED=2  
INFO: Process has 3 diagrams  
INFO: Trying process: u u~ > t t~ WEIGHTED=2  
INFO: Process has 1 diagrams  
INFO: Trying process: u c~ > t t~ WEIGHTED=2  
INFO: Trying process: c u~ > t t~ WEIGHTED=2  
INFO: Trying process: c c~ > t t~ WEIGHTED=2  
INFO: Process has 1 diagrams  
INFO: Trying process: d d~ > t t~ WEIGHTED=2  
INFO: Process has 1 diagrams  
INFO: Trying process: d s~ > t t~ WEIGHTED=2  
INFO: Trying process: s d~ > t t~ WEIGHTED=2  
INFO: Trying process: s s~ > t t~ WEIGHTED=2  
INFO: Process has 1 diagrams  
INFO: Process u~ u > t t~ added to mirror process u u~ > t t~  
INFO: Process c~ c > t t~ added to mirror process c c~ > t t~  
INFO: Process d~ d > t t~ added to mirror process d d~ > t t~  
INFO: Process s~ s > t t~ added to mirror process s s~ > t t~  
5 processes with 7 diagrams generated in 0.075 s  
Total: 5 processes with 7 diagrams
```





# Exercise 1: solution

- Which partonic subprocesses contribute?

- `> display processes`

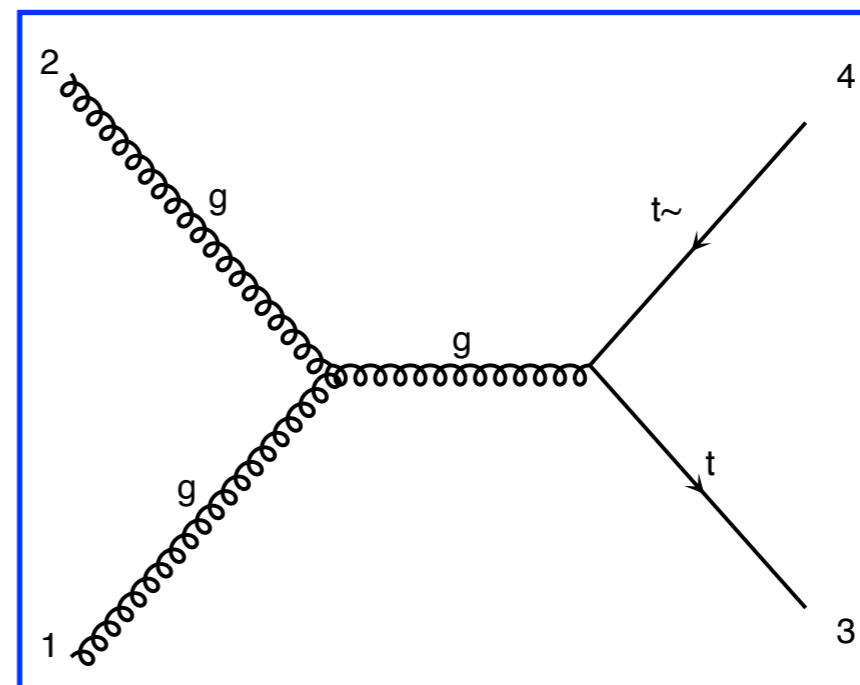
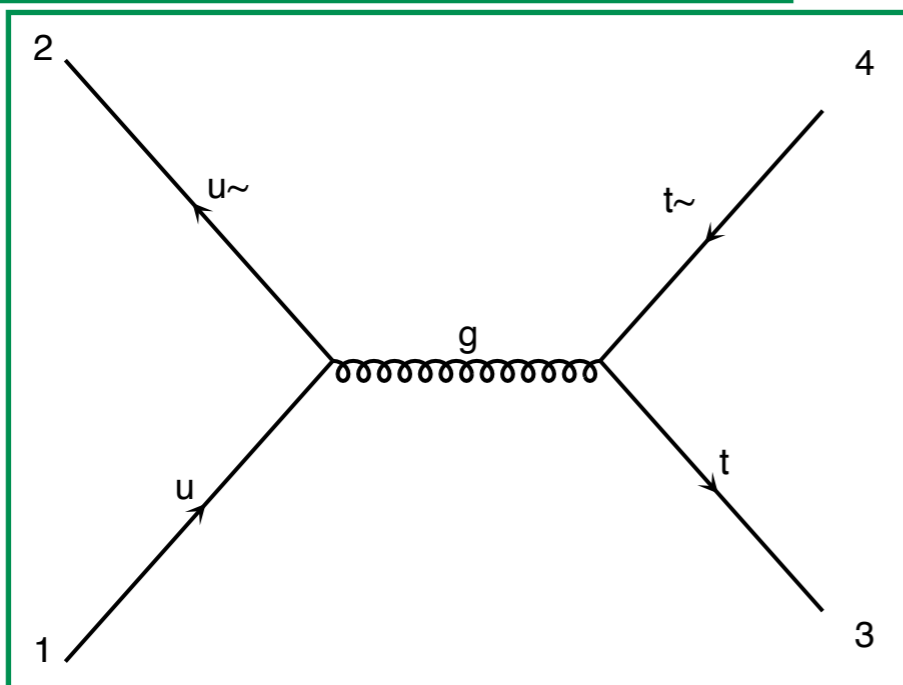
```
Process: g g > t t~ WEIGHTED=2  
Process: u u~ > t t~ WEIGHTED=2  
Process: c c~ > t t~ WEIGHTED=2  
Process: d d~ > t t~ WEIGHTED=2  
Process: s s~ > t t~ WEIGHTED=2
```

# Exercise I: solution

- Which partonic subprocesses contribute?

- > **display processes**

```
Process: g g > t t~ WEIGHTED=2  
Process: u u~ > t t~ WEIGHTED=2  
Process: c c~ > t t~ WEIGHTED=2  
Process: d d~ > t t~ WEIGHTED=2  
Process: s s~ > t t~ WEIGHTED=2
```





# Exercise I: solution

- Which partonic subprocesses contribute?

- `> display processes`

```
Process: g g > t t~ WEIGHTED=2  
Process: u u~ > t t~ WEIGHTED=2  
Process: c c~ > t t~ WEIGHTED=2  
Process: d d~ > t t~ WEIGHTED=2  
Process: s s~ > t t~ WEIGHTED=2
```

QCD master formula:

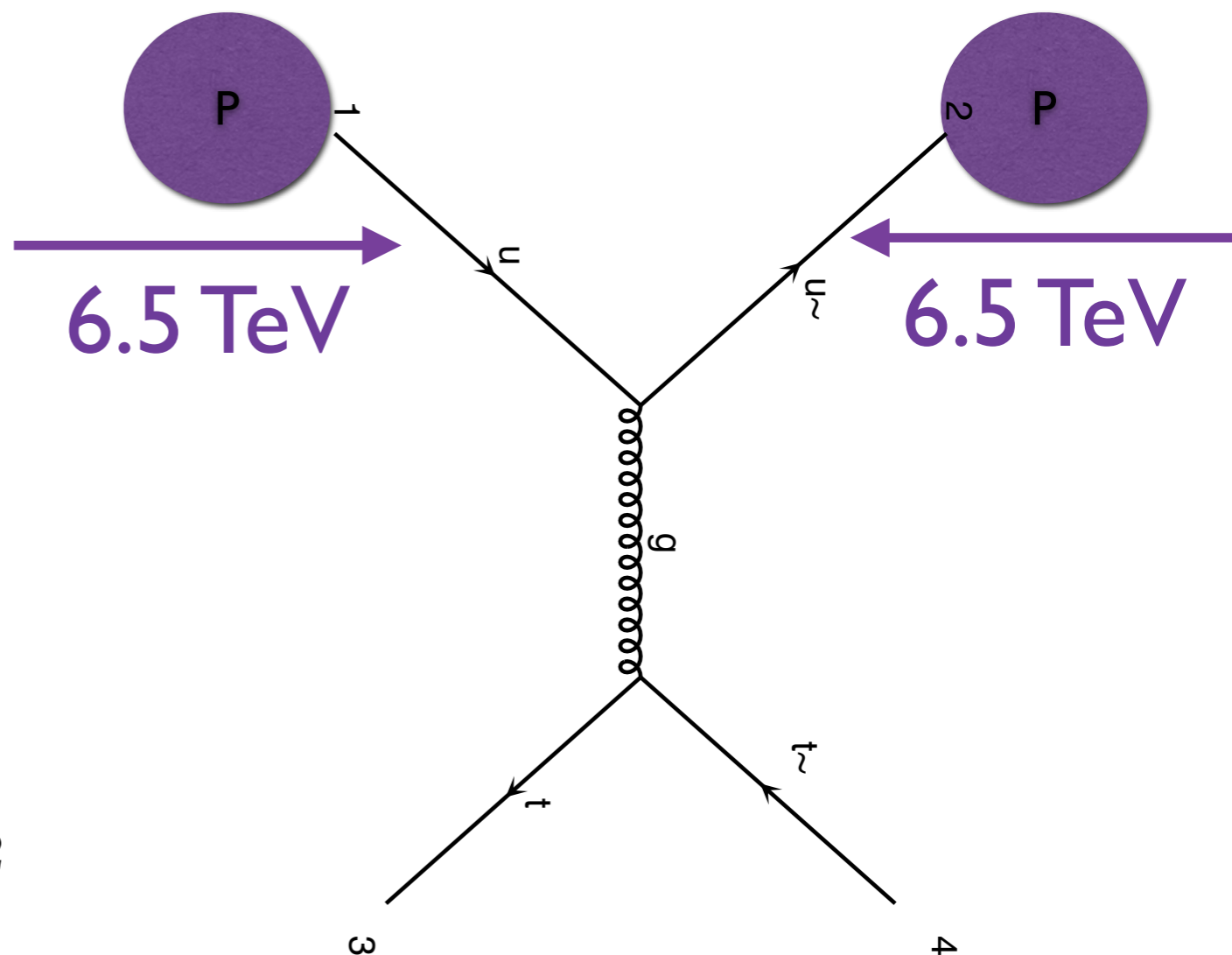
$$\sigma(pp \rightarrow t\bar{t}) = \sum_{ab} \int dx_1 dx_2 f_a(x_1, \mu_F) f_b(x_2, \mu_F) \times \hat{\sigma}(ab \rightarrow t\bar{t})$$

# What does it mean?

$$\sigma(pp \rightarrow t\bar{t}) = \sum_{ab} \int dx_1 dx_2 f_a(x_1, \mu_F) f_b(x_2, \mu_F) \times \hat{\sigma}(ab \rightarrow t\bar{t})$$

- What is the probability to find parton  $a$  inside the proton with momentum fraction  $x$ ?  $f_a(x)$
- $\mu_F$  is a scale which separates low energy from high energy dynamics
- The partonic scattering occurs at a reduced energy:

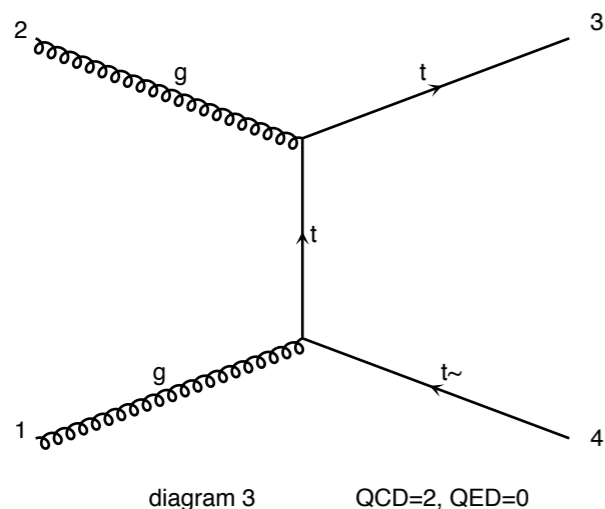
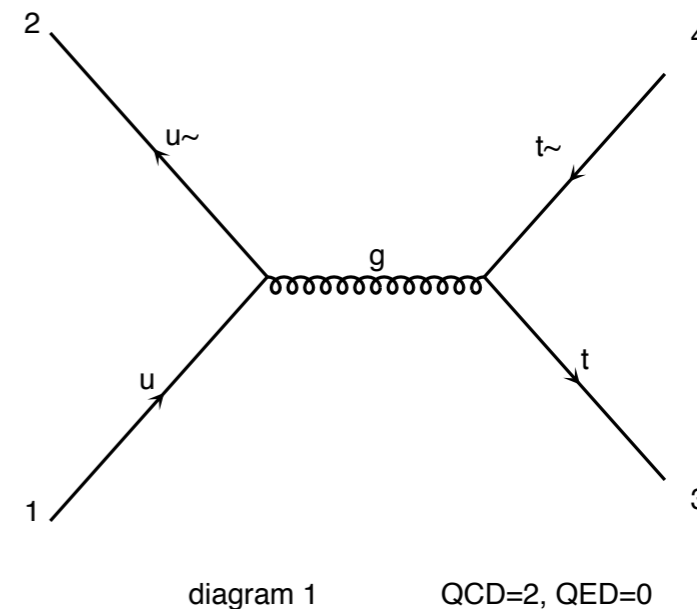
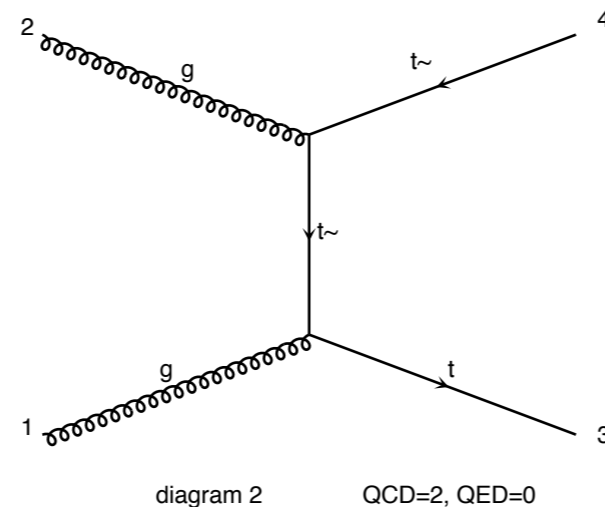
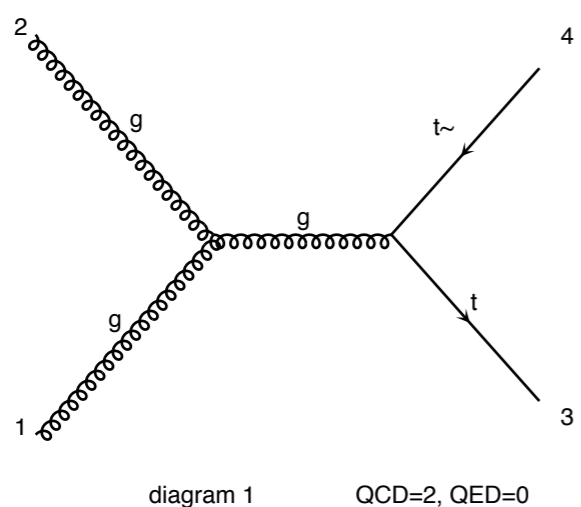
$$\hat{s} = x_1 x_2 S = x_1 x_2 (13\text{TeV})^2$$





# Exercise I: solution

- How many Feynman diagrams has each subprocess?
  - > display diagrams



gg: 3 diagrams

q $\bar{q}$ : 1 diagram



# Exercise I: solution

- Output the code

- `> output mytestdir`

```
INFO: initialize a new directory: mytestdir
INFO: remove old information in mytestdir
INFO: Creating files in directory P0_gg_ttx
INFO: Generating Feynman diagrams for Process: g g > t t~ WEIGHTED=2
INFO: Finding symmetric diagrams for subprocess group gg_ttx
INFO: Creating files in directory P0_qq_ttx
INFO: Generating Feynman diagrams for Process: u u~ > t t~ WEIGHTED=2
INFO: Finding symmetric diagrams for subprocess group qq_ttx
History written to /Users/marcozaro/Physics/MadGraph/MG5_aMC_v2_2_2/mytestdir/Cards/proc_card_mg5.dat
Generated helas calls for 2 subprocesses (0 diagrams) in 0.000 s
Wrote files for 16 helas calls in 0.102 s
Export UFO model to MG4 format
ALOHA: aloha creates FFV1 routines
ALOHA: aloha creates VVV1 set of routines with options: P0
save configuration file to /Users/marcozaro/Physics/MadGraph/MG5_aMC_v2_2_2/mytestdir/Cards/me5_configuration.txt
INFO: Use Fortran compiler gfortran
INFO: Generate jpeg diagrams
INFO: Generate web pages
Output to directory /Users/marcozaro/Physics/MadGraph/MG5_aMC_v2_2_2/mytestdir done.
```



# Exercise I: solution

- Compute the cross-section at the LHC (13.5 TeV) for  $m_t=170$  GeV

- **> launch**

The following switches determine which programs are run:

- 1 Run the pythia shower/hadronization: pythia=NOT INSTALLED
- 2 Run PGS as detector simulator: pgs=NOT INSTALLED
- 3 Run Delphes as detector simulator: delphes=NOT INSTALLED
- 4 Decay particles with the MadSpin module: madspin=OFF
- 5 Add weight to events based on coupling parameters: reweight=OFF

Either type the switch number (1 to 5) to change its default setting,  
or set any switch explicitly (e.g. type 'madspin=ON' at the prompt)

Type '0', 'auto', 'done' or just press enter when you are done.

[0, 4, 5, auto, done, madspin=ON, madspin=OFF, madspin, reweight=ON, ... ][60s to answer]

- **> 0 (let's keep it simple ;-)**

Do you want to edit a card (press enter to bypass editing)?

- 1 / param : param\_card.dat
- 2 / run : run\_card.dat

you can also

- enter the path to a valid card or banner.
  - use the 'set' command to modify a parameter directly.  
The set option works only for param\_card and run\_card.  
Type 'help set' for more information on this command.
  - call an external program (ASperGE/MadWidth/...).
- Type 'help' for the list of available command

[0, done, 1, param, 2, run, enter path][60s to answer]



# Exercise I: solution

- Compute the cross-section at the LHC (13.5 TeV) for  $m_t=170$  GeV

```

*****
# Running parameters run_card
*****
#
*****
# Tag name for the run (one word) *
#*****
tag_1 = run_tag ! name of the run
#*****
# Run to generate the grid pack *
#*****
.false. = gridpack !True = setting up the grid pack
#*****
# Number of events and rnd seed *
# Warning: Do not generate more than 1M events in a single run *
# If you want to run Pythia, avoid more than 50k events in a run. *
#*****
10000 = nevents ! Number of unweighted events requested
0 = iseed ! rnd seed (0=assigned automatically=default))
#*****
# Collider type and energy *
# lpp: 0=No PDF, 1=proton, -1=antiproton, 2=photon from proton, *
# 3=photon from electron *
#*****
1 = lpp1 ! beam 1 type
1 = lpp2 ! beam 2 type
6500 = ebeam1 ! beam 1 total energy in GeV
6500 = ebeam2 ! beam 2 total energy in GeV
#*****
# Beam polarization from -100 (left-handed) to 100 (right-handed) *
#*****
0 = polbeam1 ! beam polarization for beam 1
0 = polbeam2 ! beam polarization for beam 2
#*****
# PDF CHOICE: this automatically fixes also alpha_s and its evol. *
#*****

```

## param\_card

```

#####
## INFORMATION FOR MASS
#####
Block mass
5 4.700000e+00 # MB
6 1.730000e+02 # MT
15 1.777000e+00 # MTA
23 9.118800e+01 # MZ
25 1.250000e+02 # MH
## Dependent parameters, given by model restrictions.
## Those values should be edited following the
## analytical expression. MG5 ignores those values
## but they are important for interfacing the output of MG5
## to external program such as Pythia.
1 0.000000 # d : 0.0
2 0.000000 # u : 0.0
3 0.000000 # s : 0.0
4 0.000000 # c : 0.0
11 0.000000 # e- : 0.0
12 0.000000 # ve : 0.0
13 0.000000 # mu- : 0.0
14 0.000000 # vm : 0.0
16 0.000000 # vt : 0.0
21 0.000000 # g : 0.0
22 0.000000 # a : 0.0
24 80.419002 # w+ : cmath.sqrt(MZ__exp__2/2. + cmath.sqrt(MZ__exp__4
/4. - (aEW*cmath.pi*MZ__exp__2)/(Gf*sqrt__2)))
<_v2_2_2/mytestdir/Cards/param_card.dat" 78L, 2770C 1,1 Top

```





# Exercise 1: solution

- Compute the cross-section at the LHC (8 TeV) for  $m_t=172$  GeV
- One can also set the parameters without editing the cards (useful for scripting)
  - `> set ebeam1 6800`
  - `> set ebeam2 6800`
  - `> set MT 172.`
  - `> done`



# Exercise I: solution

- Compute the cross-section at the LHC (8 TeV) for  $m_t=172$  GeV
- One can also set the parameters without editing the cards (useful for scripting)

- `> set ebeam1 6800`
- `> set ebeam2 6800`
- `> set MT 172.`
- `> done`

```
. . .
Working on SubProcesses
  P0_gg_ttx
  P0_qq_ttx
INFO: Idle: 0, Running: 1, Completed: 1 [ current time: 15h13 ]
INFO: End survey
refine 10000
Creating Jobs
INFO: Refine results to 10000
  P0_gg_ttx
  P0_qq_ttx
INFO: Idle: 6, Running: 4, Completed: 3 [ 3.2s ]
INFO: Idle: 2, Running: 4, Completed: 7 [ 6.6s ]
INFO: Idle: 0, Running: 1, Completed: 12 [ 9.7s ]
INFO: Combining runs
INFO: finish refine
refine 10000
Creating Jobs
INFO: Refine results to 10000
  P0_gg_ttx
  P0_qq_ttx
INFO: Combining runs
INFO: finish refine
combine_events
INFO: Combining Events
=== Results Summary for run: run_01 tag: tag_1 ===

Cross-section : 160.1 +- 0.2302 pb ←
Nb of events : 10000
```



# Monitor via the web interface

Results in the sm for  $p p > t t \sim$

## Currently Running

Run Name	Tag Name	Cards	Results	Status/Jobs		
				Queued	Running	Done
run_01	tag_1	<a href="#">param card</a> <a href="#">run card</a> <a href="#">plot card</a>	<a href="#">160.1 ± 0.2302 (pb)</a>	Combining Events		

## Available Results

Run	Collider	Banner	Cross section (pb)	Events	Data	Output	Action
run_01	$p p$ 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">160.1 ± 0.23</a>	No events yet		banner only	<input type="button" value="remove run"/> <input type="button" value="re-run from the banner"/>

[Main Page](#)



# Exercise I: solution

- Script it:
  - open a text file (`mymg5amc.txt`) and put the commands inside:

```
generate p p > t t~  
output mytestdir  
launch  
set ebeam1 6800  
set ebeam2 6800  
set MT 172
```
  - launch `MG5_aMC@NLO` with that file
  - `./bin/mg5 amc mymg5amc.txt`



# Exercise I:

## Extra questions:

- Are b-quarks included in the initial state? If not, how can I include them?

- `> display processes`

```
Process: g g > t t~ WEIGHTED=2  
Process: u u~ > t t~ WEIGHTED=2  
Process: c c~ > t t~ WEIGHTED=2  
Process: d d~ > t t~ WEIGHTED=2  
Process: s s~ > t t~ WEIGHTED=2
```

- No b-quark appears. Note that at the startup you have

```
Defined multiparticle p = g u c d s u~ c~ d~ s~  
Defined multiparticle j = g u c d s u~ c~ d~ s~
```

- You can add the  $b/\bar{b}$  to the multiparticle labels

- `> define p = p b b~`

```
Defined multiparticle p = g u c d s u~ c~ d~ s~ b b~
```

- `> display multiparticles`

- For consistency one should use a model with  $m_b=0$

- `> import model sm-no_b_mass`



# Exercise I:

## Extra questions:



# Exercise 1:

## Extra questions:

- Are b-quarks included in the initial state? If not, how can I include them?



# Exercise I:

## Extra questions:

- Are b-quarks included in the initial state? If not, how can I include them?
- Regenerate the process
  - `> generate p p > t t~`
  - `> display processes`

```
Process: g g > t t~ WEIGHTED=2  
Process: u u~ > t t~ WEIGHTED=2  
Process: c c~ > t t~ WEIGHTED=2  
Process: d d~ > t t~ WEIGHTED=2  
Process: s s~ > t t~ WEIGHTED=2  
Process: b b~ > t t~ WEIGHTED=2
```








# Exercise I:

## Extra questions:

- Are b-quarks included in the initial state? If not, how can I include them?
- Regenerate the process
  - `> generate p p > t t~`
  - `> display processes`

```
Process: g g > t t~ WEIGHTED=2
Process: u u~ > t t~ WEIGHTED=2
Process: c c~ > t t~ WEIGHTED=2
Process: d d~ > t t~ WEIGHTED=2
Process: s s~ > t t~ WEIGHTED=2
Process: b b~ > t t~ WEIGHTED=2
```
- Does it make a big difference? 
  - `> output`
  - `> launch`
  - `> set ebeam1 4000`
  - `> set ebeam2 4000`
  - `> set MT 172`



# Exercise I:

## Extra questions:

- Are b-quarks included in the initial state? If not, how can I include them?

- Regenerate the process

- `> generate p p > t t~`

- `> display processes`

```
Process: g g > t t~ WEIGHTED=2  
Process: u u~ > t t~ WEIGHTED=2  
Process: c c~ > t t~ WEIGHTED=2  
Process: d d~ > t t~ WEIGHTED=2  
Process: s s~ > t t~ WEIGHTED=2  
Process: b b~ > t t~ WEIGHTED=2
```

- Does it make a big difference? 

- `> output`

- `> launch`

- `> set ebeam1 4000`

- `> set ebeam2 4000`

- `> set MT 172`

```
Cross-section : 160.4 +- 0.231 pb  
Nb of events : 10000
```

Without b

```
Cross-section : 160.1 +- 0.2302 pb  
Nb of events : 10000
```



# Exercise I:

## Extra questions:



# Exercise I:

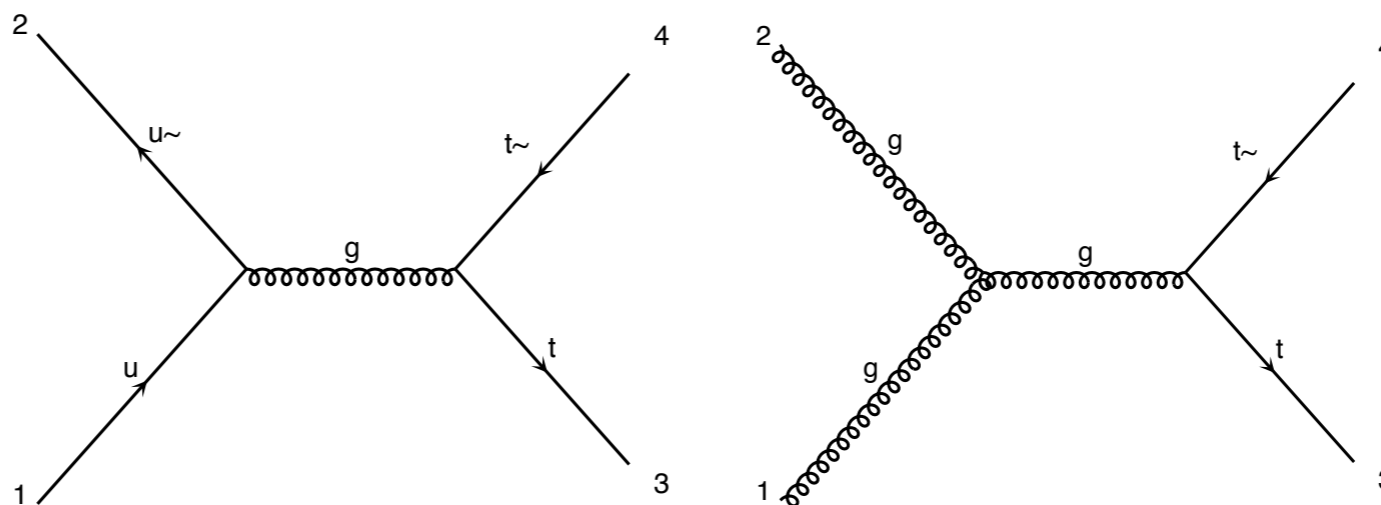
## Extra questions:

- Are diagrams with photons/ $z$  included? If not, how can I include them? How much does the cross-section change? What is that 'WEIGHTED'?

# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change? What is that ‘WEIGHTED’?
- > **display diagrams**



- No photon/z appear.
- Are we missing anything important?



# Exercise I:

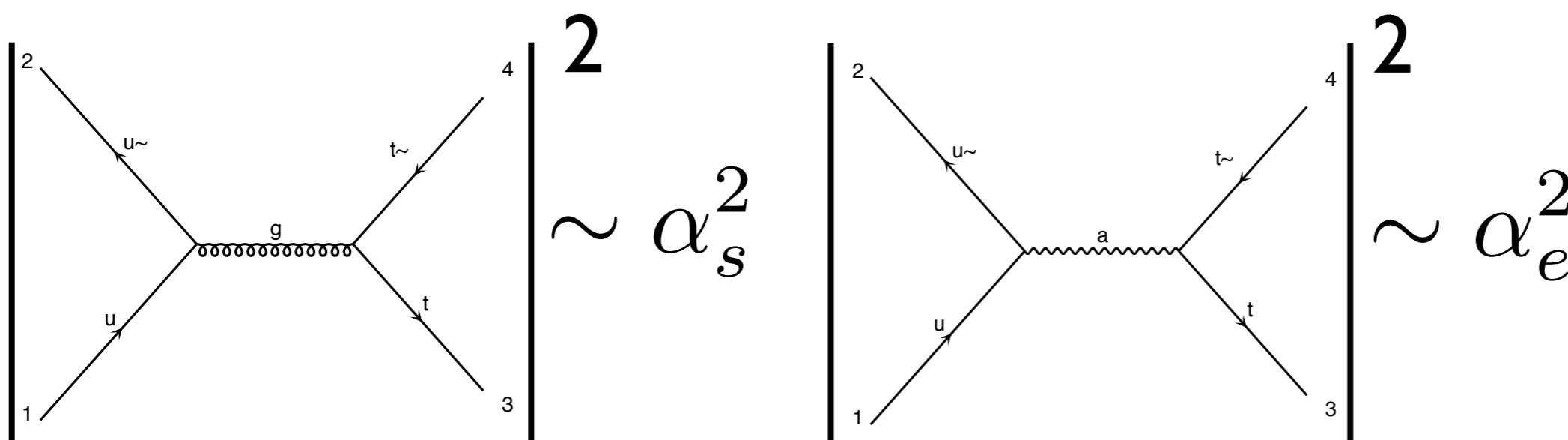
## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change? What is that ‘WEIGHTED’?
  - `> display diagrams`
  - No photon/z appear.
  - Are we missing anything important?

# Exercise I:

## Extra questions:

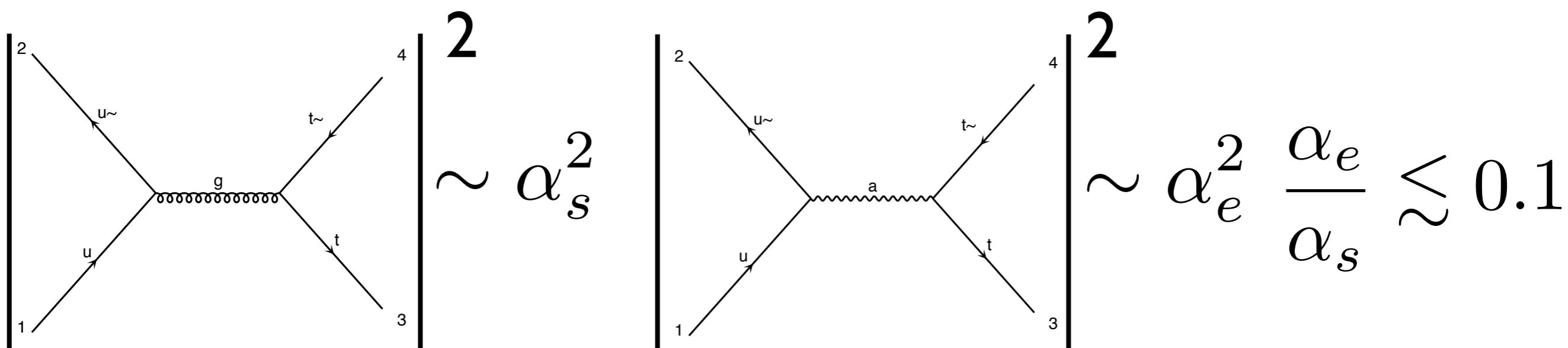
- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change? What is that ‘WEIGHTED’?
  - > **display diagrams**
  - No photon/z appear.
  - Are we missing anything important?



# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change? What is that ‘WEIGHTED’?
  - > **display diagrams**
  - No photon/z appear.
  - Are we missing anything important?







# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change?  
What is 'WEIGHTED'?
  - > `display diagrams`
  - No photon/z appear.
  - Are we missing anything important? Does not seem the case
  - How to have them anyway?
  - MG5 exploits the hierarchy between QCD and QED couplings in order to give the leading (i.e. with most QCD) contribution to the cross-section by default
  - It assign WEIGHTED order = 1 (=2) to QCD (QED) vertices and generates the process with minimum WEIGHTED order



# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change?

What is 'WEIGHTED'?

- > `display diagrams`
- No photon/z appear.
- Are we missing anything important? Does not seem the case
- How to have them anyway?
- MG5 exploits the hierarchy between QCD and QED couplings in order to give the leading (i.e. with most QCD) contribution to the cross-section by default
- It assign WEIGHTED order = 1 (=2) to QCD (QED) vertices and generates the process with minimum WEIGHTED order



# Exercise I:

## Extra questions:



# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change?
  - > `generate p p > t t~ WEIGHTED=4`
  - > `display diagrams`



# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change?
  - > generate `pp > tt~ WEIGHTED=4`
  - > display diagrams

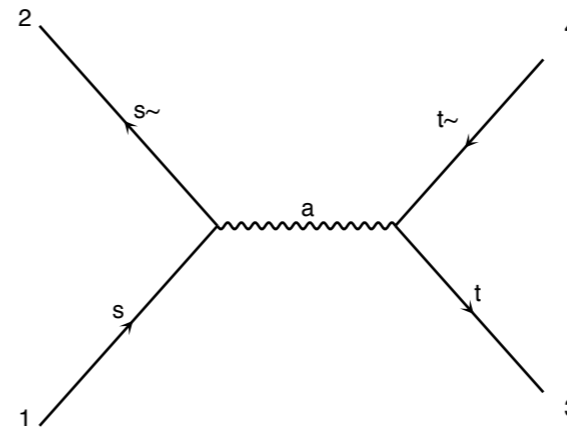


diagram 1 QCD=0, QED=2

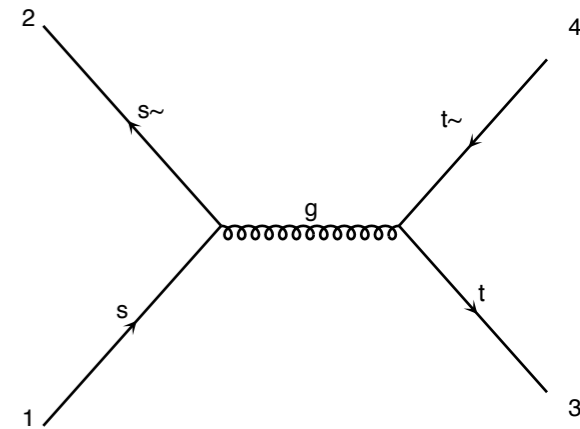


diagram 2 QCD=2, QED=0

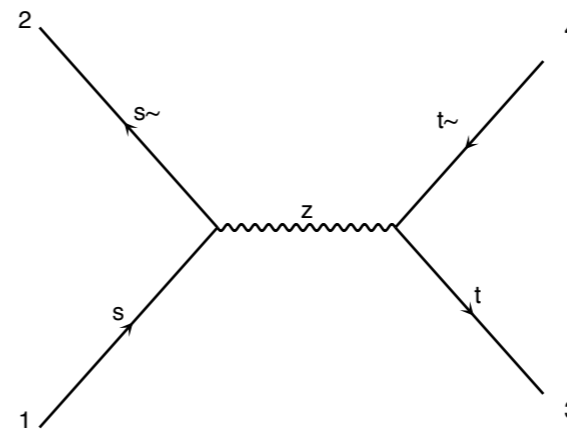


diagram 3 QCD=0, QED=2



# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change?
  - > generate p p > t t~ WEIGHTED=4
  - > display diagrams
  - > output ...
  - > launch
  - > ...

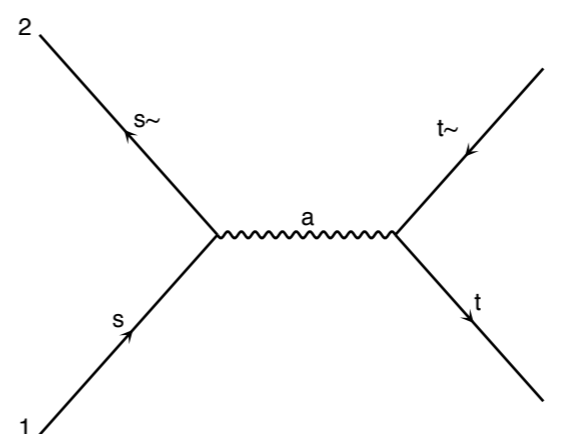


diagram 1 QCD=0, QED=2

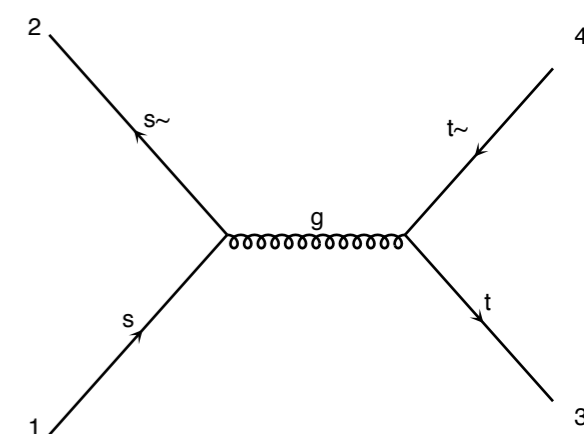


diagram 2 QCD=2, QED=0

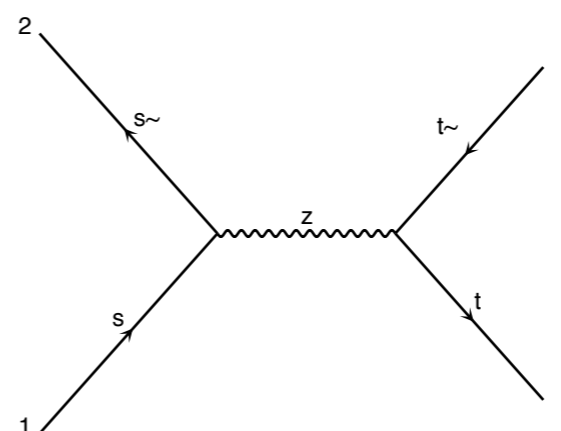


diagram 3 QCD=0, QED=2



# Exercise I:

## Extra questions:

- Are diagrams with photons/z included? If not, how can I include them? How much does the cross-section change?
  - > generate p p > t t~ WEIGHTED=4
  - > display diagrams
  - > output ...
  - > launch
  - > ...

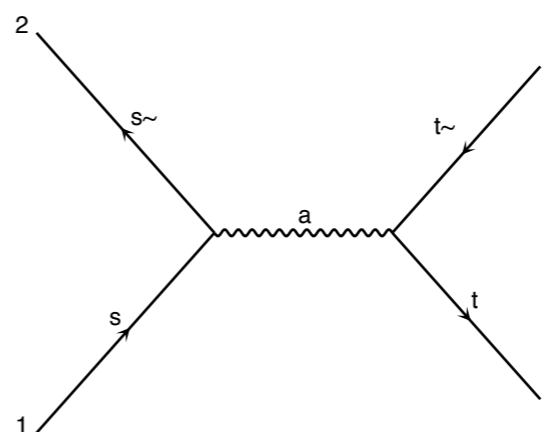


diagram 1 QCD=0, QED=2

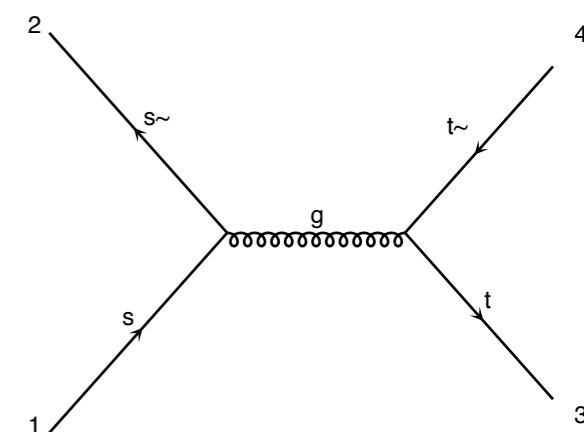


diagram 2 QCD=2, QED=0

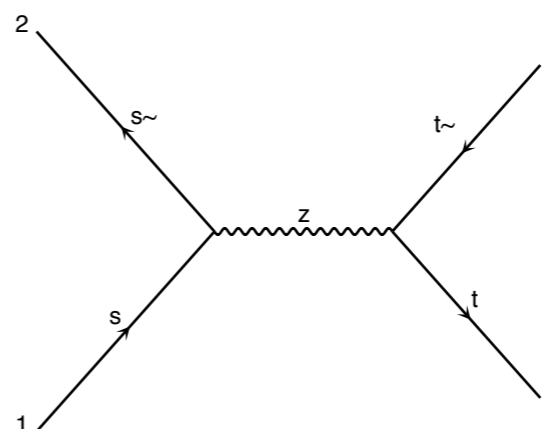


diagram 3 QCD=0, QED=2

Cross-section : 160.8 +- 0.1999 pb  
 Nb of events : 10000

WEIGHTED=2

Cross-section : 160.4 +- 0.231 pb  
 Nb of events : 10000



# Exercise I:

## Extra questions:





# Exercise I:

## Extra questions:

- Alternatively, one can specify the coupling powers
  - $>$  generate  $p p > t t \sim$  QED=2
  - orders which are not specified are unconstrained



# Exercise I:

## Extra questions:

- Alternatively, one can specify the coupling powers
  - $>$  generate  $p p \rightarrow t t^{\sim}$  QED=2
  - orders which are not specified are unconstrained
- In order to have only the QED contribution
  - $>$  generate  $p p \rightarrow t t^{\sim}$  QED=2 QCD=0



# Exercise I:

## Extra questions:

- Recompute the  $t\bar{t}$  cross-section for  $m_t=170, 172, 174 \dots 180$  GeV
- Be smart! Script it!
- Create a txt file `myttbar_scan.txt`

```
generate p p > t t~
output mytestdir2
launch
set ebeam1 4000
set ebeam2 4000
set MT 170
launch
set MT 172
launch
set MT 174
launch
set MT 176
launch
set MT 178
launch
set MT 180
```

- `./bin/mg5_aMC myttbar_scan.txt`



# Exercise I:

## Extra questions:

- Recompute the  $t\bar{t}$  cross-section for  $m_t=170, 172, 174 \dots 180$  GeV
- Be smart! Script it!
- You can also launch an existing folder, without regenerating the code

```
launch mytestdir2  
set ebeam1 4000  
set ebeam2 4000  
set MT 170  
launch  
set MT 172  
launch  
set MT 174  
launch  
set MT 176  
launch  
set MT 178  
launch  
set MT 180
```





# Exercise I:

## Extra questions:

- Recompute the  $t\bar{t}$  cross-section for  $m_t=170, 172, 174 \dots 180$  GeV

Results in the sm for  $p p > t t\sim$

### Available Results

Run	Collider	Banner	Cross section (pb)	Events	Data	Output	Action
run_01	$p p$ 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">169.8 ± 0.24</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_02	$p p$ 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">160.1 ± 0.28</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_03	$p p$ 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">151.1 ± 0.2</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_04	$p p$ 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">142.9 ± 0.18</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_05	$p p$ 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">134.7 ± 0.19</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_06	$p p$ 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">127.3 ± 0.16</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>

[Main Page](#)



# Exercise I:

## Extra questions:

- Recompute the  $t\bar{t}$  cross-section for  $m_t=170, 172, 174 \dots 180$  GeV

Results in the sm for  $p p > t t\sim$

### Available Results

Run	Collider	Banner	Cross section (pb)	Events	Data	Output	Action
run_01	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">169.8 ± 0.24</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_02	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">160.1 ± 0.28</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_03	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">151.1 ± 0.2</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_04	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">142.9 ± 0.18</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_05	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">134.7 ± 0.19</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_06	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">127.3 ± 0.16</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>

[Main Page](#)

↑  
which folder is what?



# Exercise I:

## Extra questions:

- Recompute the  $t\bar{t}$  cross-section for  $m_t=170, 172, 174 \dots 180$  GeV
- Be smart! Script it!
- You can specify the name (instead of `run_01...`) with `-n NAME`

```
launch mytestdir2 -n run_MT170  
set ebeam1 4000  
set ebeam2 4000  
set MT 170  
launch -n run_MT172  
set MT 172  
launch -n run_MT174  
set MT 174  
launch -n run_MT176  
set MT 176  
launch -n run_MT178  
set MT 178  
launch -n run_MT180  
set MT 180
```



# Exercise I:

## Extra questions:

- Recompute the  $t\bar{t}$  cross-section for  $m_t=170, 172, 174 \dots 180$  GeV

Run	Collider	Banner	Cross section (pb)	Events	Data	Output	Action
run_01	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">169.8 ± 0.24</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_02	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">160.1 ± 0.28</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_03	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">151.1 ± 0.2</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_04	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">142.9 ± 0.18</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_05	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">134.7 ± 0.19</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_06	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">127.3 ± 0.16</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_MT170	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">170 ± 0.22</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_MT172	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">159.6 ± 0.22</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_MT174	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">151.1 ± 0.22</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_MT176	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">142.6 ± 0.19</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_MT178	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">134.7 ± 0.18</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_MT180	p p 4000 x 4000 GeV	<a href="#">tag_1</a>	<a href="#">127.2 ± 0.24</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>

[Main Page](#)





# Exercise 2: decay chains

- Theory: the top quark is an unstable particle:
  - It decays:  $\sim 100\%$  of times into  $b W$
  - The  $W$  boson decays too:
    - 67% ( $2/3$ ) of times into hadrons
    - 22% ( $2/9$ ) of times into “leptons” ( $e-\nu_e$  or  $\mu-\nu_\mu$ )
    - 11% ( $1/9$ ) of times into  $\tau-\nu_\tau$
- A decayed pair of top quarks can be classified as:
  - hadronic (both tops to hadrons)
  - semileptonic (one top to hadrons, the other to leptons)
  - dileptonic (both quarks to leptons)



# Exercise 2: decay chains

- **Questions:**
  - How often a top pair decays hadronically/semi-leptonically/di-leptonically?
  - Learn the syntax to specify decay chains
  - Generate the code for dileptonic top decay and compute the cross-section. Compare with the case where the top does not decay (leave all parameters as default)
  - Compute the cross section for  $m_t=170, 175$  and  $180$  GeV. Do you see anything strange?
  - What is the difference with  $p p \rightarrow l^+ l^- \nu_l \bar{\nu}_l b \bar{b}$ ?



# Exercise 2: Solution



**Top Pair Decay Channels**

$\bar{c}s$	electron+jets	muon+jets	tau+jets	all-hadronic	
$\bar{u}d$					
$\tau^-$	$e\tau$	$\mu\tau$	$\tau\tau$	tau+jets	
$\mu^-$	$e\mu$	$\mu\mu$	$\mu\tau$	muon+jets	
$e^-$	$e\tau$	$e\mu$	$e\tau$	electron+jets	
$W^-$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$



# Exercise 2: Solution

- Questions:
  - How often a top pair decays hadronically/semi-leptonically/di-leptonically?
  - Since the top always decays to  $Wb$ , look at how a pair of  $W$  decays (b's are stable)

### Top Pair Decay Channels

$c\bar{s}$	electron+jets	muon+jets	tau+jets	all-hadronic	
$u\bar{d}$					
$\tau^-$					
$\mu^-$	$e\mu$	$\mu\mu$	$\mu\tau$	muon+jets	
$e^-$	$e\tau$	$e\mu$	$e\tau$	electron+jets	
$W$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$



# Exercise 2: Solution

- Questions:
  - How often a top pair decays hadronically/semi-leptonically/di-leptonically?
  - Since the top always decays to  $Wb$ , look at how a pair of  $W$  decays (b's are stable)
  - **Hadronically:  $2/3 * 2/3 = 4/9$**

### Top Pair Decay Channels

$c\bar{s}$	electron+jets	muon+jets	tau+jets	all-hadronic	
$u\bar{d}$					
$\tau^-$					
$\mu^-$	$e\mu$	$\mu\mu$	$\mu\tau$	muon+jets	
$e^-$	$e\tau$	$e\mu$	$e\tau$	electron+jets	
$W$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$



# Exercise 2: Solution

- Questions:
  - How often a top pair decays hadronically/semi-leptonically/di-leptonically?
  - Since the top always decays to  $Wb$ , look at how a pair of  $W$  decays (b's are stable)
  - **Hadronically:  $2/3 * 2/3 = 4/9$**

**Top Pair Decay Channels**

$c\bar{s}$	electron+jets	muon+jets	tau+jets	all-hadronic	
$u\bar{d}$					
$\tau^-$					
$\mu^-$	$e\mu$	$\mu\mu$	$\tau\mu$	muon+jets	
$e^-$	$e\tau$	$e\mu$	$e\tau$	electron+jets	
$W$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$



# Exercise 2: Solution

- Questions:
  - How often a top pair decays hadronically/semi-leptonically/di-leptonically?
    - Since the top always decays to  $Wb$ , look at how a pair of  $W$  decays (b's are stable)
    - **Hadronically:  $2/3 * 2/3 = 4/9$**
    - **Semi-lep. (incl.  $\tau$ ):  $2 * 1/3 * 2/3 = 4/9$**

**Top Pair Decay Channels**

$\bar{c}s$	electron+jets	muon+jets	tau+jets	all-hadronic	
$\bar{u}d$					
$\tau^-$					
$\mu^-$	e $\mu$	$\mu\mu$	$\mu\tau$	muon+jets	
$e^-$	e $e$	e $\mu$	e $\tau$	electron+jets	
$W$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$

# Exercise 2: Solution

- Questions:
  - How often a top pair decays hadronically/semi-leptonically/di-leptonically?
    - Since the top always decays to  $Wb$ , look at how a pair of  $W$  decays (b's are stable)
    - **Hadronically:  $2/3 * 2/3 = 4/9$**
    - **Semi-lep. (incl.  $\tau$ ):  $2 * 1/3 * 2/3 = 4/9$**
    - **Di-lep. (incl.  $\tau$ ):  $1/3 * 1/3 = 1/9$**

**Top Pair Decay Channels**

$\bar{c}s$	electron+jets	muon+jets	tau+jets	all-hadronic	
$\bar{u}d$					
$\tau^-$	$e\tau$	$\mu\tau$	$\tau\tau$		
$\mu^-$	$e\mu$	$\mu\mu$	$\mu\tau$	muon+jets	
$e^-$	$e\mu$	$e\mu$	$e\tau$	electron+jets	
$W$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$





# Exercise 2: Solution

- Questions:

- Learn the syntax to specify decay chains
- > **help generate**

-- generate diagrams for a given process

General leading-order syntax:

o generate INITIAL STATE > REQ S-CHANNEL > FINAL STATE \$ EXCL S-CHANNEL / FORBIDDEN PARTICLES COUP1=ORDER1 COUP2^2=ORDER2 @N

o Example: generate l+ vl > w+ > l+ vl a \$ z / a h QED=3 QCD=0 @1

> Alternative required s-channels can be separated by "|":

b b~ > W+ W- | H+ H- > ta+ vt ta- vt~

> If no coupling orders are given, MG5 will try to determine orders to ensure maximum number of QCD vertices.

> Desired coupling orders combination can be specified directly for the squared matrix element by appending '^2' to the coupling name. For example, 'p p > j j QED^2==2 QCD^2==2' selects the QED-QCD interference terms only. The other two operators '<=' and '>' are supported. Finally, a negative value COUP^2==-I refers to the N^(-I+1)L0 term in the expansion of the COUP order.

> To generate a second process use the "add process" command

Decay chain syntax:

o core process, decay1, (decay2, (decay2', ...)), ... etc

o Example: generate p p > t~ t QED=0, (t~ > W- b~, W- > l- vl~), t > j j b @2

> Note that identical particles will all be decayed

- > **generate p p > t t~, (t > w+ b, w+ > l+ vl), (t~ > w- b~, w- > l- vl~)**

Something like this!





# Exercise 2: Solution





# Exercise 2: Solution

- Questions:
  - Generate the code for dileptonic top decay and compute the cross-section. Compare with what computed in Ex. I



# Exercise 2: Solution

- Questions:
  - Generate the code for dileptonic top decay and compute the cross-section. Compare with what computed in Ex. 1
    - `> generate p p > t t~, (t > w+ b, w+ > l+ vl), (t~ > w- b~, w- > l- vl~)`
    - `> output myttbardecayed`
    - `> launch`
  - What do we expect?
    - Something like  $505 * 1/9 = 56 \text{ pb}$ ?
  - Wait: what is  $1+/1-$ ?



# Exercise 2: Solution

- Questions:
  - Generate the code for dileptonic top decay and compute the cross-section. Compare with what computed in Ex. 1
    - `> generate p p > t t~, (t > w+ b, w+ > l+ vl), (t~ > w- b~, w- > l- vl~)`
    - `> output myttbardecayed`
    - `> launch`
  - What do we expect?
    - Something like  $505 * 1/9 = 56 \text{ pb}$ ?
  - Wait: what is  $l^+/l^-$ ?
    - `> display multi particles`

Multiparticle labels:

```
all = g u c d s u~ c~ d~ s~ a ve vm vt e- mu- ve~ vm~ vt~ e+ mu+
t b t~ b~ z w+ h w- ta- ta+
l- = e- mu-
j = g u c d s u~ c~ d~ s~
vl = ve vm vt
l+ = e+ mu+
p = g u c d s u~ c~ d~ s~
vl~ = ve~ vm~ vt~
```



# Exercise 2: Solution

- Questions:

- Generate the code for dileptonic top decay and compute the cross-section. Compare with what computed in Ex. I

- `> generate p p > t t~, (t > w+ b, w+ > l+ vl), (t~ > w- b~, w- > l- vl~)`
- `> output myttbardecayed`
- `> launch`

- What do we expect?  $4/81 = 25$

- Something like  $505 * \cancel{1/9} = 56$  pb?

- Wait: what is  $l+ / l-?$

- `> display multi particles`

Cross-section : 22.63 +- 0.01553 pb  
Nb of events : 10000

Multiparticle labels:

```
all = g u c d s u~ c~ d~ s~ a ve vm vt e- mu- ve~ vm~ vt~ e+ mu+
t b t~ b~ z w+ h w- ta- ta+
l- = e- mu-
j = g u c d s u~ c~ d~ s~
vl = ve vm vt
l+ = e+ mu+
p = g u c d s u~ c~ d~ s~
vl~ = ve~ vm~ vt~
```

last bit of discrepancy comes from  
more subtle things  
(essentially scales)



# Exercise 2: Solution

- Questions:
  - Compute the cross section for  $m_t=170, 175$  and  $180$  GeV. Do you see anything strange?

## Available Results

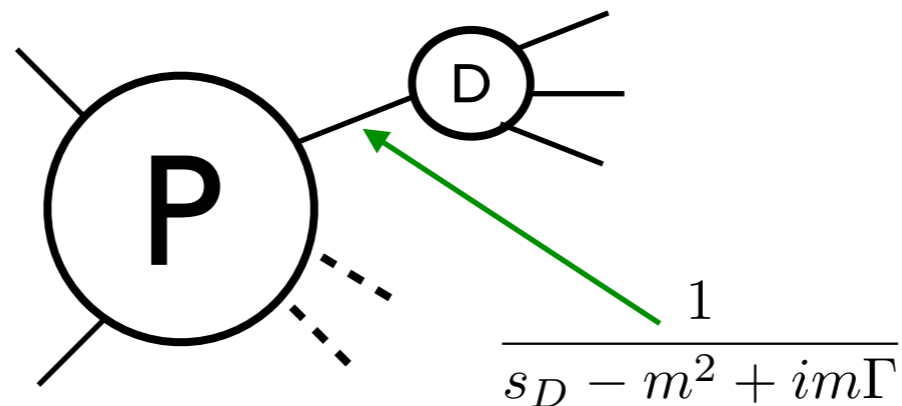
launch run\_170  
set mt 170  
done  
launch run\_175  
set mt 175  
done  
launch run\_180  
set mt 180  
done

Run	Collider	Banner	Cross section (pb)	Events	Data	Output	Action
run_170	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">21.83 ± 0.061</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_175	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">23.41 ± 0.064</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>
run_180	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">24.92 ± 0.058</a>	10000	parton madevent	<a href="#">LHE</a>	<input type="button" value="remove run"/> <input type="button" value="launch detector simulation"/>

[Main Page](#)

- The cross section grows with  $m_t$ !?!

# What is happening?



$$\begin{aligned} \sigma_{P \times D} &= \int d\text{PS} |M_P|^2 \frac{1}{(s_D - m^2)^2 + m^2 \Gamma^2} |M_D|^2 \\ &= \int d\text{PS} |M_P|^2 \frac{\pi}{m\Gamma} \delta(s_D - m^2) |M_D|^2 + \mathcal{O}(\Gamma^0) \end{aligned}$$

**The total width  $\Gamma$  depends on  $m$  and should be updated!**





# Exercise 2: Solution

- Questions:
  - Compute the cross section for  $m_t=170, 175$  and  $180$  GeV. Do you see anything strange?

```

launch run_170_gammaok
set mt 170
set wt auto
done
launch run_175_gammaok
set mt 175
set wt auto
done
launch run_180_gammaok
set mt 180
set wt auto
done

```

run_170	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">21.83 ± 0.061</a>	10000	parton madevent	<a href="#">LHE</a>
run_175	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">23.41 ± 0.064</a>	10000	parton madevent	<a href="#">LHE</a>
run_180	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">24.92 ± 0.058</a>	10000	parton madevent	<a href="#">LHE</a>
run_170_gammaok	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">24.71 ± 0.071</a>	10000	parton madevent	<a href="#">LHE</a>
run_175_gammaok	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">21.54 ± 0.064</a>	10000	parton madevent	<a href="#">LHE</a>
run_180_gammaok	pp 6500.0 x 6500.0 GeV	<a href="#">tag_1</a>	<a href="#">18.8 ± 0.05</a>	10000	parton madevent	<a href="#">LHE</a>

- With “set wt auto” the top width is re-computed from the param\_card parameters



# Exercise 2: Solution

- Questions:
  - What is the difference with  $p_{p > 1+} - p_{p > 1-}$   $v_{1+} - v_{1-}$   $b_{p > 1+} - b_{p > 1-}$ ?



# Exercise 2: Solution

- Questions:
  - What is the difference with  $p \rightarrow l^+ l^- \nu l \bar{\nu} b \bar{b}$ ?
  - It is a much more complex process (will not run in 10s on a laptop)
    - Each subprocess has  $O(100)$  diagrams rather than  $O(1)$

# Exercise 2: Solution

- Questions:

- What is the difference with  $p p \rightarrow l^+ l^- \nu l \nu l \sim b b \sim$ ?

- It is a much more complex process (will not run in 10s on a laptop)
  - Each subprocess has  $O(100)$  diagrams rather than  $O(1)$
  - This process ‘contains’  $t\bar{t}$  decayed, but also other things

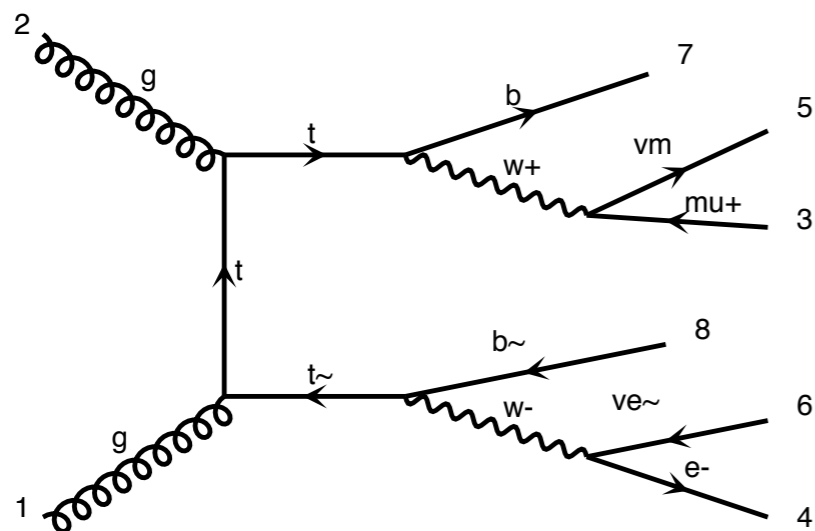
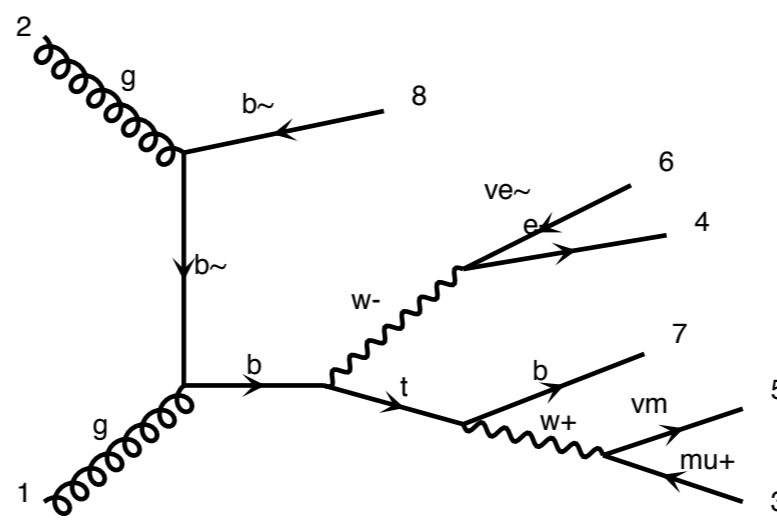


diagram 81



QCD=2, QED=4

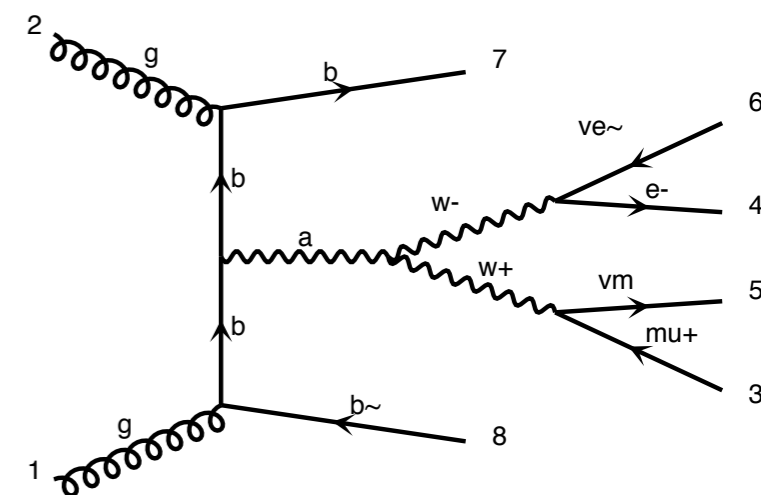


diagram 46

QCD=2, QED=4



# Exercise 2: Solution

- Questions:
  - What is the difference with  $p \rightarrow l^+ l^- \nu l \bar{\nu} b$   $b \rightarrow \bar{\nu} \nu$ ?
  - It is a much more complex process (will not run in 10s on a laptop)
    - Each subprocess has  $O(100)$  diagrams rather than  $O(1)$
    - This process 'contains'  $t\bar{t}$  decayed, but also other things
  - Which one is correct?



# Exercise 2: Solution

- Questions:
  - What is the difference with  $p \rightarrow l^+ l^- \nu_l \bar{\nu}_l \sim b \bar{b}$ ?
    - It is a much more complex process (will not run in 10s on a laptop)
      - Each subprocess has  $O(100)$  diagrams rather than  $O(1)$
      - This process 'contains'  $t\bar{t}$  decayed, but also other things
  - Which one is correct?
    - Strictly speaking  $t\bar{t}$  decayed, is correct only in the limit  $\Gamma_t=0$  i.e. when tops are on-shell



# Exercise 2: Solution

- Questions:
  - What is the difference with  $p \rightarrow l^+ l^- \nu l \sim b \bar{b}$ ?
    - It is a much more complex process (will not run in 10s on a laptop)
      - Each subprocess has  $O(100)$  diagrams rather than  $O(1)$
      - This process 'contains'  $t\bar{t}$  decayed, but also other things
  - Which one is correct?
    - Strictly speaking  $t\bar{t}$  decayed, is correct only in the limit  $\Gamma_t=0$  i.e. when tops are on-shell
    - If one searches for (on-shell) top-pair production (e.g. imposing cuts on  $l, \nu, b$  mass), the full process will give little extra contribution



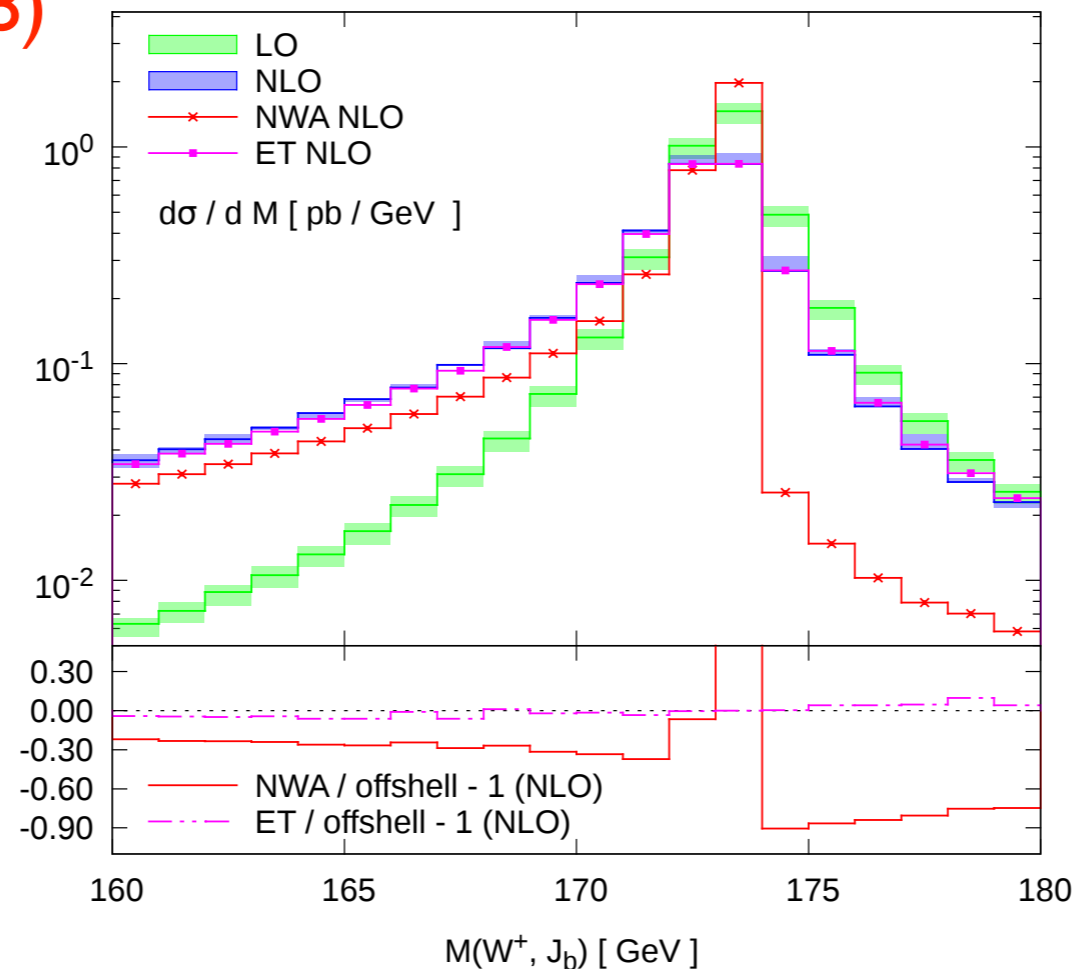
# Exercise 2: Solution

- Questions:
  - What is the difference with  $p \rightarrow l^+ l^- \nu l \sim b \bar{b}$ ?
    - It is a much more complex process (will not run in 10s on a laptop)
      - Each subprocess has  $O(100)$  diagrams rather than  $O(1)$
      - This process 'contains'  $t\bar{t}$  decayed, but also other things
  - Which one is correct?
    - Strictly speaking  $t\bar{t}$  decayed, is correct only in the limit  $\Gamma_t=0$  i.e. when tops are on-shell
    - If one searches for (on-shell) top-pair production (e.g. imposing cuts on  $l, \nu, b$  mass), the full process will give little extra contribution
    - If one wants to look away from the resonant region, then the full



# Exercise 2: Solution

- Questions:
  - What is the difference with  $p p \rightarrow l^+ l^- \nu l \nu l \sim b \bar{b}$ ?
  - Have a look at single-top production ([Papanastasiou et al. arXiv:1305.7088](#))





## Exercise 3:

# Unitarity in gauge theories

- Consider the process  $e^+e^- \rightarrow W^+W^-$ :
  - Which diagrams contribute?
    - Generate the full process, the process with no ZWW vertex and the process with only the neutrino diagram
    - Use the `/ x y` syntax in the `generate` command to veto specific particles (see also `help generate`)
  - Calculate the cross section at  $\sqrt{s}=165, 175, \dots, 205, 400$  GeV (script it!) and comment the behaviour  
*Hint: set `ebeam 200` sets both beams' energies to 200*

# Exercise 3:

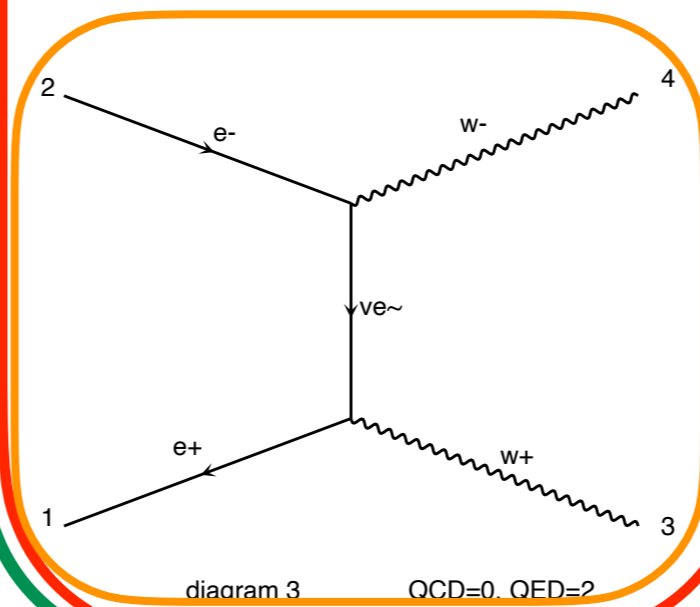
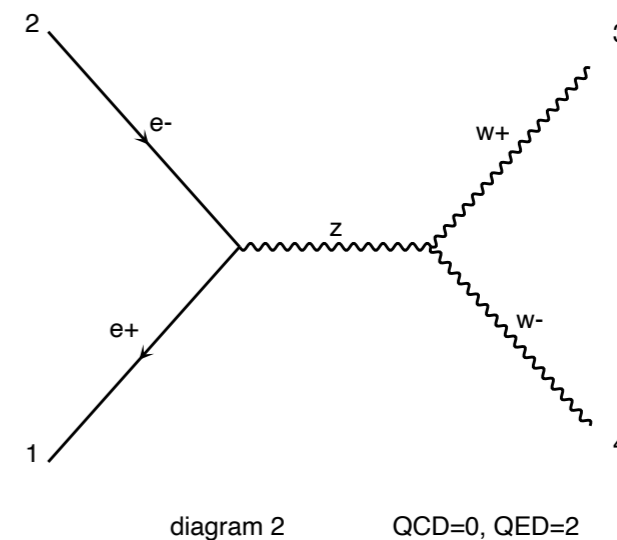
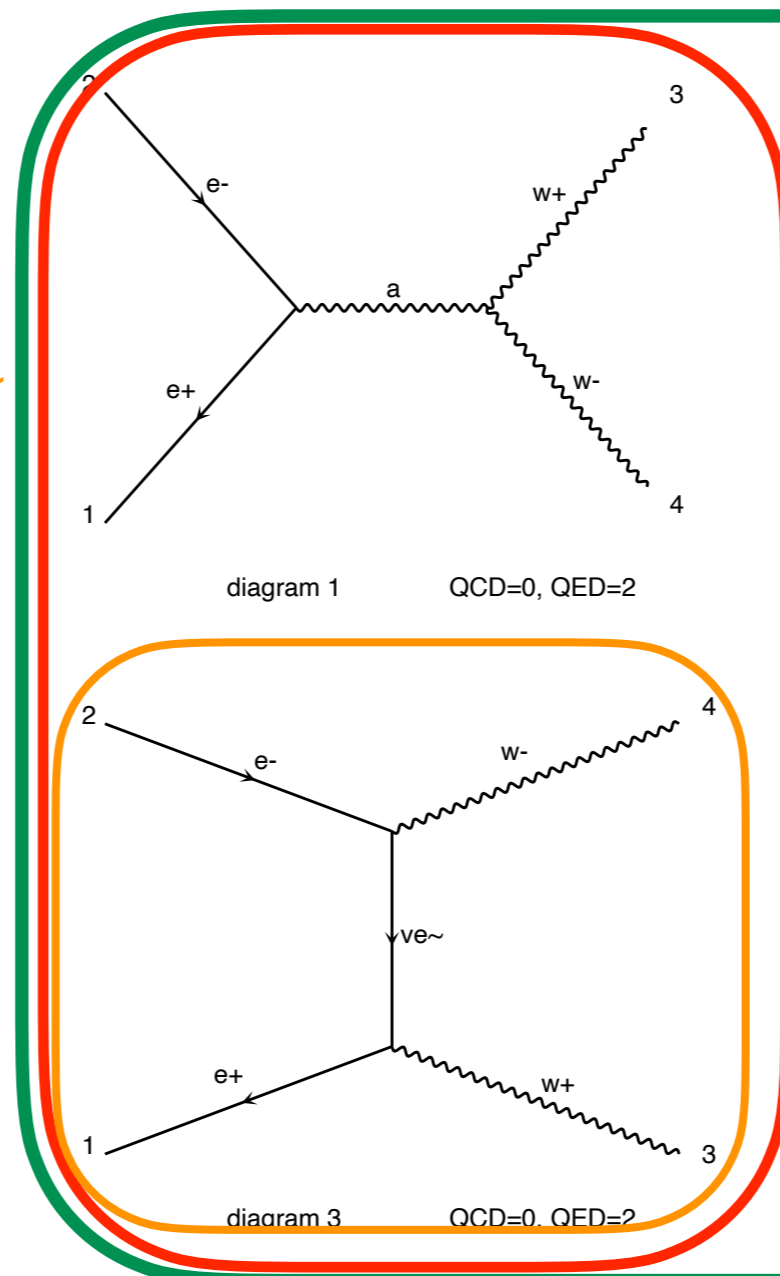
## Unitarity in gauge theories

### Feynman Diagrams:

generate  $e^+ e^- \rightarrow w^+ w^-$

generate  $e^+ e^- \rightarrow w^+ w^- / z$

generate  $e^+ e^- \rightarrow w^+ w^- / z a$





## Exercise 3:

# Unitarity in gauge theories

- Script to calculate the cross sections

```
generate_events run_165
set ebeam 82.5
generate_events run_175
set ebeam 87.5
generate_events run_185
set ebeam 92.5
generate_events run_195
set ebeam 97.5
generate_events run_205
set ebeam 102.5
generate_events run_400
set ebeam 200
```

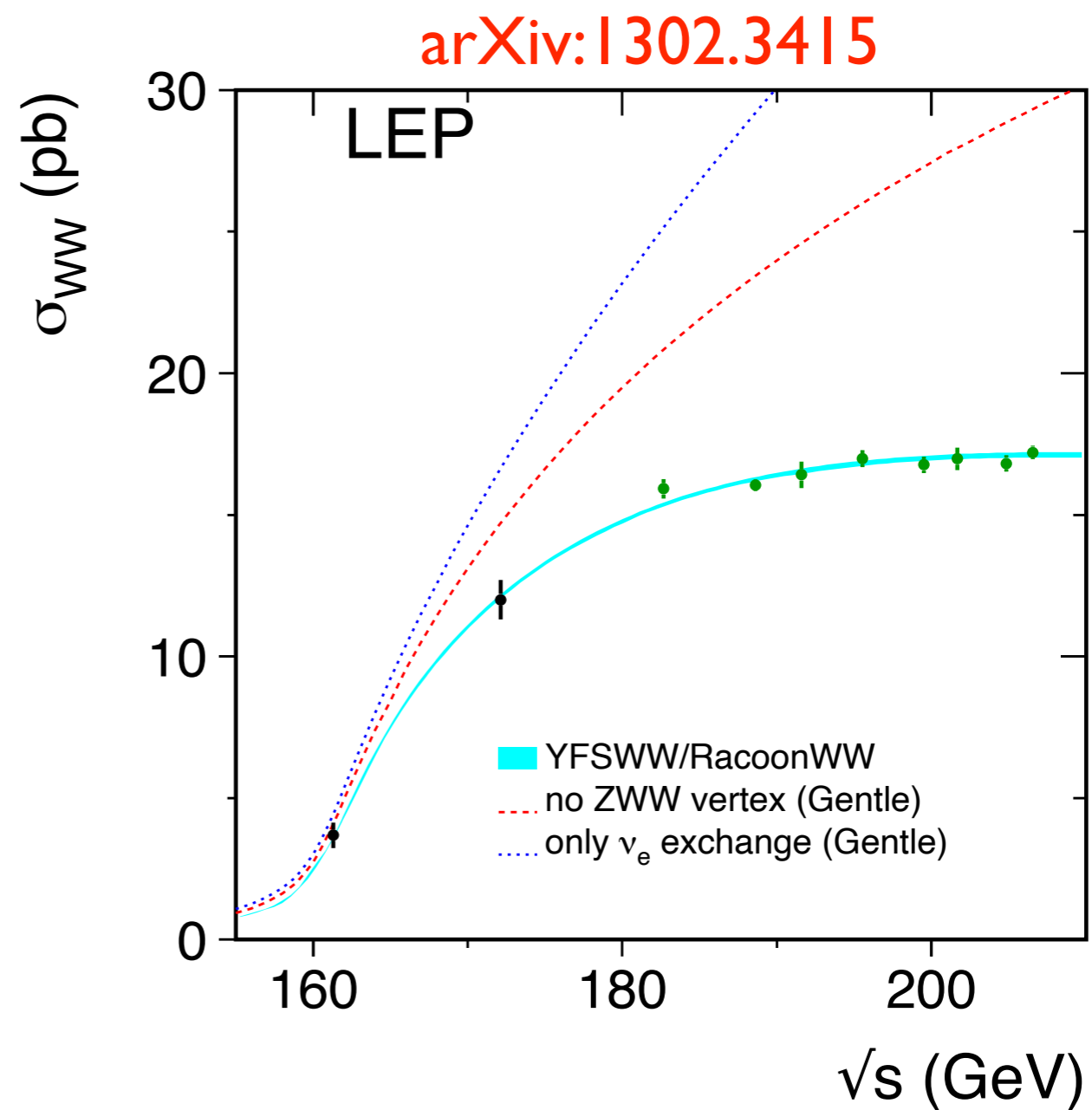
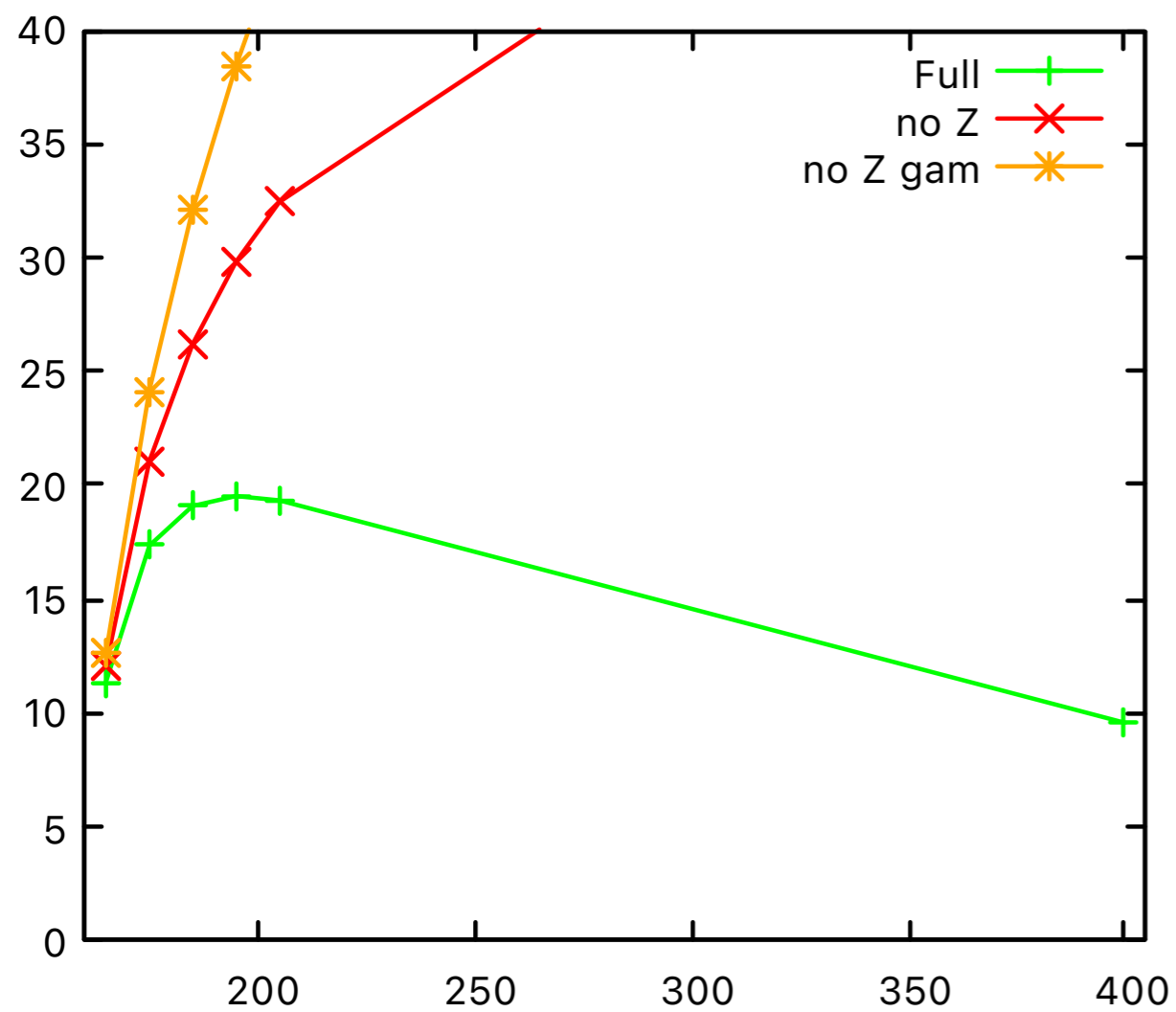
# Exercise 3:

## Unitarity in gauge theories

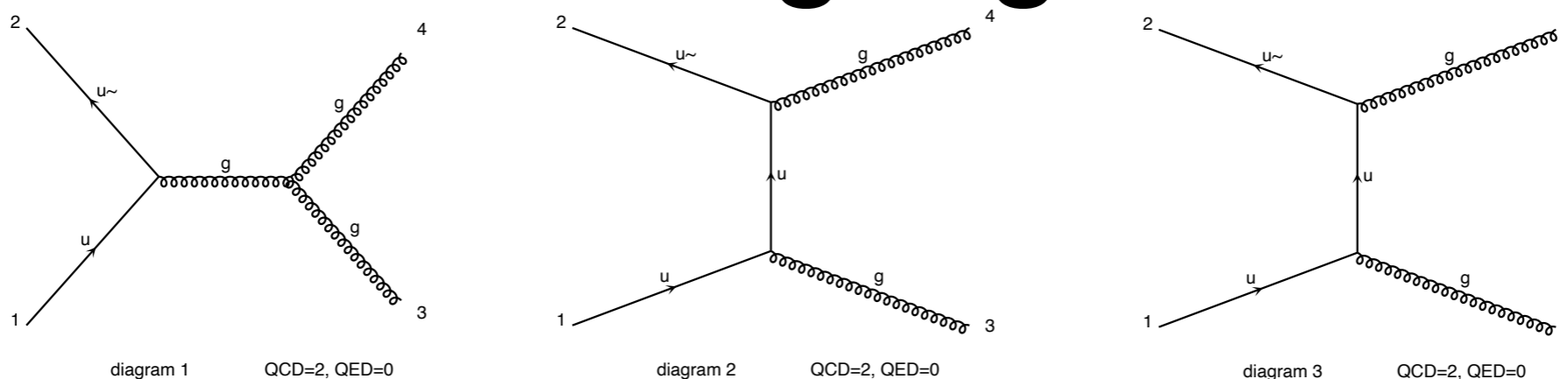
- Results

$e^+ e^- \rightarrow w^+ w^-$   $e^+ e^- \rightarrow w^+ w^- / z$   $e^+ e^- \rightarrow w^+ w^- / z a$

Run	Collider	Banner	Cross section (pb)	Cross section (pb)	Cross section (pb)
run_165	$e^+ e^-$ 82.5 x 82.5 GeV	<a href="#">tag_1</a>	<a href="#">11.38 ± 0.021</a>	<a href="#">12.09 ± 0.019</a>	<a href="#">12.66 ± 0.016</a>
run_175	$e^+ e^-$ 87.5 x 87.5 GeV	<a href="#">tag_1</a>	<a href="#">17.37 ± 0.04</a>	<a href="#">21.07 ± 0.032</a>	<a href="#">24.18 ± 0.043</a>
run_185	$e^+ e^-$ 92.5 x 92.5 GeV	<a href="#">tag_1</a>	<a href="#">19.1 ± 0.043</a>	<a href="#">26.19 ± 0.045</a>	<a href="#">32.07 ± 0.043</a>
run_195	$e^+ e^-$ 97.5 x 97.5 GeV	<a href="#">tag_1</a>	<a href="#">19.53 ± 0.061</a>	<a href="#">29.8 ± 0.057</a>	<a href="#">38.39 ± 0.056</a>
run_205	$e^+ e^-$ 102.5 x 102.5 GeV	<a href="#">tag_1</a>	<a href="#">19.35 ± 0.064</a>	<a href="#">32.43 ± 0.071</a>	<a href="#">43.73 ± 0.054</a>
run_400	$e^+ e^-$ 200.0 x 200.0 GeV	<a href="#">tag_1</a>	<a href="#">9.579 ± 0.03</a>	<a href="#">57.02 ± 0.074</a>	<a href="#">101.8 ± 0.13</a>



# What's going on?



- Consider a simpler case  $u\bar{u} \rightarrow gg$  in QCD:
  - In a non-abelian gauge theory, in order to fulfil the Ward identity  $\mathcal{M}^{\mu_3\mu_4} p_{\mu_3} \varepsilon_{\mu_4} = 0$  one must include the diagram with the 3-gauge vertex
 
$$\mathcal{M}_2^{\mu_3\mu_4} \sim g^2 t^{a_3} t^{a_4} \quad \mathcal{M}_3^{\mu_3\mu_4} \sim -g^2 t^{a_4} t^{a_3} \quad \mathcal{M}_1^{\mu_3\mu_4} \sim g^2 f^{a_3 a_4 b} t^b$$
  - Otherwise, the Ward identity is violated
    - no gauge invariance
    - possible violation of unitarity at high energies: in the case with the  $W$ 's, the longitudinal component has terms  $\sim E/m_W$ , whose contribution cancels in a gauge invariant amplitude



## Exercise 4:

# Initial-state radiation in lepton collisions

- Consider muon-pair production at an electron-positron collider of 500 GeV.
- Set `pdlabel=isronly11` and `lpp1(2)=-3(+3)` in the `run_card`. This will tell the code to include ISR effects for the electrons
- Plot the invariant mass of the muon pair (MadAnalysis5 does it automatically). What do you see? How do you explain the double peak?

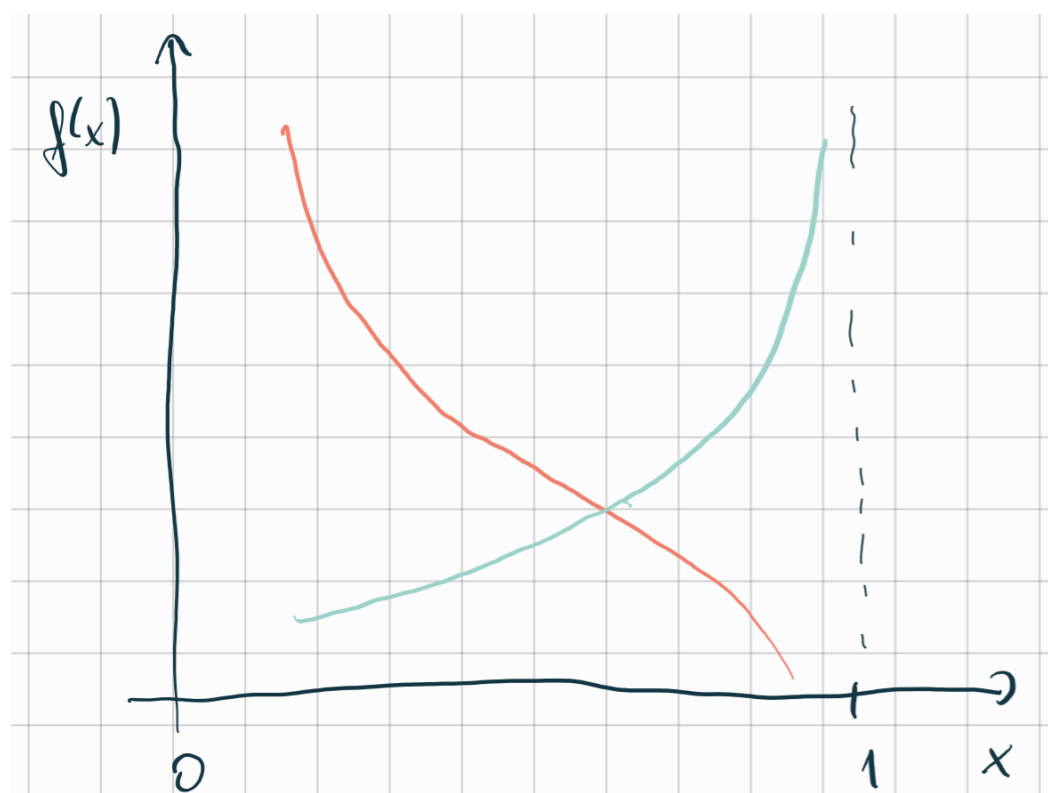


# ISR (at LL)

GRIBOV V. N. and LIPATOV L. N.  
Sov. J. Nucl. Phys., 15 (1972) 438

$$D_{GL}(x, Q^2) = \frac{\exp[(1/2)\eta(3/4 - \gamma_E)]}{\Gamma(1 + (1/2)\eta)} \frac{1}{2} \eta (1-x)^{(1/2)\eta-1} \simeq \frac{1}{(1-x)^{1-\eta/2}}$$

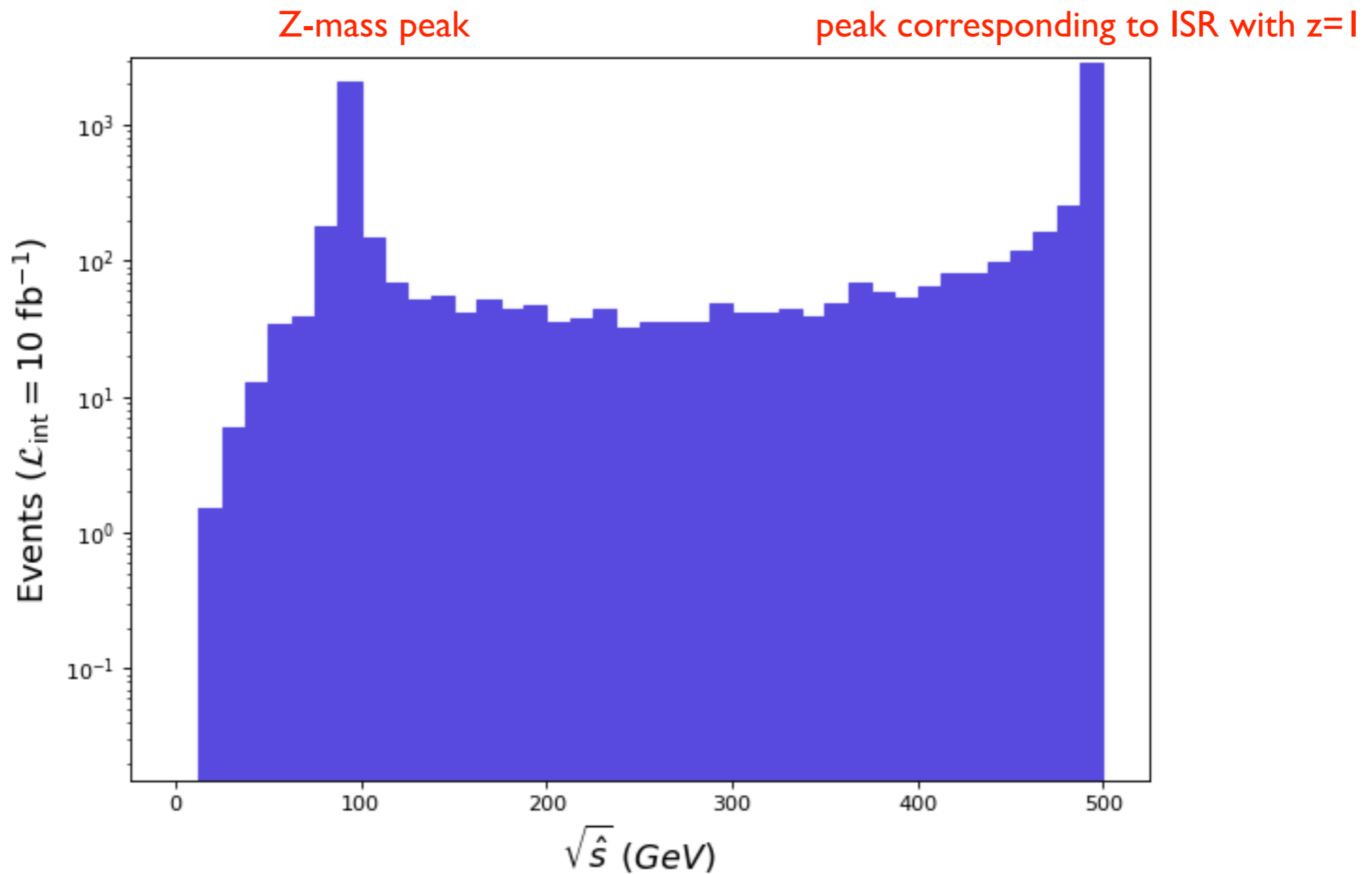
$$\left( \eta = \frac{2\alpha}{\pi} \log \frac{Q^2}{m^2} \right) \sim 0.05 \text{ for } Q=100 \text{ GeV}$$



- **Hadronic PDFs** vanish at large  $x$  (divergence at small- $x$  avoided by cuts)
- **Leptonic PDFs** diverge (but are integrable) at large  $x$
- While leptonic PDFs have been substantially improved since 1972, the asymptotic behaviour is unchanged
- A different phase space mapping is required wrt pp collisions



# Exercise 4: Solution

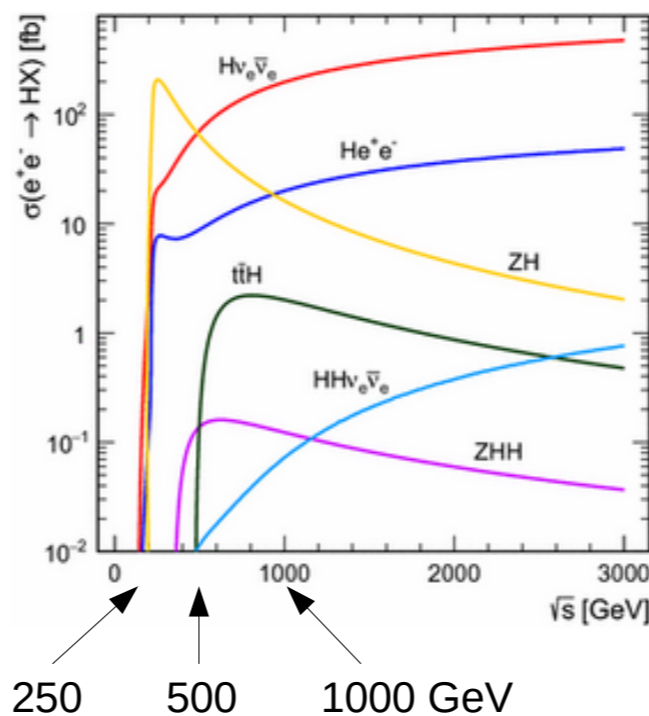
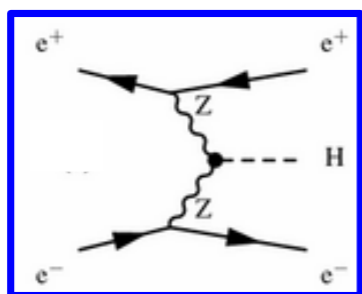
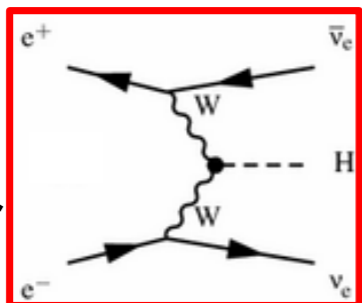
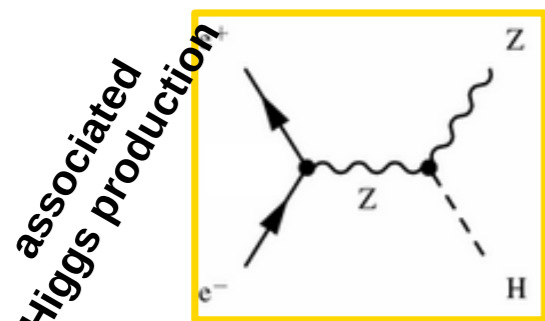


# Exercise 5:

## Higgs production at the ILC

- Try to reproduce some of the curves in this plot

Higgs production in electron-positron collisions



Higgs studies can start at **250 GeV**  
 full set of Higgs measurements:  
 add **~500 & ~1000 GeV**

